

(c) Find the slope and hence the equation of the tangent to the curve  $y = (3x - 2)(1 - x^2)$  at the point  $(0, -2)$ .

(d) Find the coordinates of the local maximum of the curve  $y = 4x^3 - 3x + 4$ .

4. (a) If  $y = \frac{x^2 - 4}{2x - 3}$ , find the value of  $\frac{dy}{dx}$  when  $x = 0$ .

(b) If  $y = (2x - 1)(x^2 - 2)$ , find the values of  $x$  for which  $\frac{dy}{dx} = 0$ .

(c) Find the slope of the tangent to the curve  $y = (2x^2 - 4x)^3$  at  $x = 1$ .

(d) The distance  $s$  metres travelled by a body in  $t$  seconds is given by the formula

$$s = 3 - 6t + 2t^3.$$

(i) Find the speed of the body after 2 seconds.

(ii) Show that the body is stopped when  $t = 1$ .

(iii) Find the acceleration after 3 seconds.

5. (a) Differentiate  $2 - 3x - x^2$  with respect to  $x$  from first principles.

(b) Find the point on the curve  $y = 4x - x^2$  at which the slope of the tangent to the curve is 1.

(c) Find the coordinates of the local maximum of the function  $y = x^3 - 9x^2 + 24x - 20$ .

6. (a) If  $y = (2x - 3)^3$ , find the value of  $\frac{dy}{dx}$  when  $x = 1$ .

(b) Show that  $(1, -5)$  is a point of the curve  $y = 2x^2 - 5x - 2$ , and find the equation of the tangent to the curve at this point.

(c) Show that the curve  $y = x^3 - 3x + 5$  has a local minimum at the point  $(1, 3)$ . Find the coordinates of the local maximum.

7. (a) Differentiate  $3x^2 - x + 4$  with respect to  $x$  from first principles.

(b) If  $y = (1 - 3x^2)^6$ , find the value of  $\frac{dy}{dx}$  when  $x = -1$ .

(c) Find the slope and hence the equation of the tangent to the curve  $y = (1 - x^2)(2x - 3)$  at the point  $(0, -3)$ .

(d) A particle moves along a straight line so that its distance  $s$  metres from a fixed point  $o$  after  $t$  seconds is given by  $s = t^3 + t^2 + 2t - 5$ . Find

(i) its speed after 1 second

(ii) the acceleration when  $t = 2$

(iii) after how many seconds is the acceleration  $8 \text{ m/sec}^2$ ?

8. (a) If  $y = (x^2 - 2)(3x - 1)$ , find the value of  $\frac{dy}{dx}$  at  $x = 0$ .

(b) Differentiate  $\frac{1}{x - x^2}$  with respect to  $x$ .